

De Broglie relations:

$$E = \hbar\omega = hf$$

$$\vec{p} = \hbar\vec{k}, \quad k = 2\pi/\lambda$$

Ionic bonding energy:

$$E_B = \frac{Q^2}{4\pi\epsilon_0} \frac{\alpha}{r}$$

Volume of a unit cell:

$$V = \vec{a}_1 \cdot (\vec{a}_2 \times \vec{a}_3)$$

Distance of net planes in an orthorhombic system:

$$d_{hkl}^2 = \frac{1}{(h/a)^2 + (k/b)^2 + (l/c)^2}$$

Bragg equation:

$$2d_{hkl} \sin \Theta = n\lambda$$

Structure factor:

$$F_{hkl} = \sum_j f_j e^{2\pi i(h\alpha_j + k\beta_j + l\gamma_j)}$$

with

$$\vec{r}_j = \alpha_j \vec{a}_1 + \beta_j \vec{a}_2 + \gamma_j \vec{a}_3$$

Dispersion relation of lattice vibrations for a two atomic chain ( $a = 2d$ ):

$$\omega_{\pm}^2(k) = \frac{C(m_1 + m_2)}{m_1 m_2} \left[ 1 \pm \sqrt{1 - \frac{4m_1 m_2}{(m_1 + m_2)^2} \sin^2\left(\frac{ka}{2}\right)} \right]$$

$\omega_+$ : optical branch

$\omega_-$ : acoustic branch

Sound velocity = Group velocity of acoustic phonons at  $k=0$ :

$$v_G = \left. \frac{\partial \omega}{\partial k} \right|_{k=0} = d \sqrt{\frac{C}{m}} = \sqrt{\frac{E}{\rho}}$$

Energy of a particle with mass  $m$ :

$$E = \frac{p^2}{2m} = \frac{\hbar^2 k^2}{2m}$$

Effective mass of an electron:

$$m_{\text{eff}} = \hbar^2 \left( \frac{\partial^2 E}{\partial k^2} \right)^{-1}$$

Fermi energy of a free electron gas:

$$E_F = \frac{\hbar^2}{2m} (3\pi^2 n)^{2/3}$$

Fermi velocity:

$$v_F = \frac{\hbar}{m} (3\pi^2 n)^{1/3}$$

Density of states:

$$D(E) = \frac{1}{2\pi^2} \left( \frac{2m}{\hbar^2} \right)^{3/2} \sqrt{E}$$

Boltzmann distribution:

$$F_B = e^{\frac{E-E_0}{k_B T}}$$

Fermi-Dirac distribution:

$$F_F = \frac{1}{e^{\frac{E-E_F}{k_B T}} + 1}$$

Current density:

$$\vec{j} = \sigma \vec{E}$$

Drift velocity:

$$\vec{v}_D = -\mu \vec{E}$$

Mobility:

$$\mu = \frac{e}{m} \tau$$

Conductivity:

$$\sigma = 1/\rho = ne\mu$$

Relaxation time:

$$\tau = \frac{\sigma m}{ne^2}$$

Electron density in the conduction band of a semiconductor:

$$n(T) = N_C e^{-\frac{E_C - E_F}{k_B T}}$$

Intrinsic electron density in a semiconductor:

$$n_i(T) = \sqrt{N_C N_V} e^{-\frac{E_C - E_V}{2k_B T}} = n_{i0} T^{3/2} e^{-\frac{E_C - E_V}{2k_B T}}$$

$$A_V = 6.02 \cdot 10^{23} \text{ particles/mol}$$

$$c = 3 \cdot 10^8 \text{ m/s}$$

$$\hbar = h/(2\pi) = 1.0545 \cdot 10^{-34} \text{ Js} = 6.5821 \cdot 10^{-16} \text{ eVs}$$

$$k_B = 1.38 \cdot 10^{-23} \text{ J/K} = 8.614 \cdot 10^{-5} \text{ eV/K}$$

$$\varepsilon_0 = 8.86 \cdot 10^{-12} \text{ C/(Vm)}$$

$$e = 1.602 \cdot 10^{-19} \text{ As}$$

$$m_e = 9.11 \cdot 10^{-31} \text{ kg}$$